| Name | Student ID No. |
|---|---|
| <u>Directions:</u> | |
| • There are 5 multiple choice questions worth each, and 2 free response questions. | 7 points each, 4 true or false questions worth 4 points |
| • You must show your work on all questions. | |
| • You must give a clear and correct explanation tions to receive credit. | n or provide a counter-example for the true/false ques- |
| • Partial credit is only available on the free res | ponse problems. |
| • Read all the questions carefully. No calculator that do symbolic algebra may be used. | rs with QWERTY keyboards or ones like TI-89 or TI-92 |
| | an orderly fashion. Box your final answers. No partial is given, or if it unclear which answer is meant to be |
| Honor | Statement |
| this exam. This includes any use of a graphing calc. School of Mathematical and Statistical Sciences and this exam with anyone in any section of MAT 272 to | her given nor received any unauthorized assistance on culator beyond those uses specifically authorized by the lyour instructor. Furthermore, you agree not to discuss until the exam testing period is over. In addition, your hecked at any time and cleared by any exam proctor. |
| Signature: | |
| Date: | |

- 1. The radius and center of the sphere $x^2 + y^2 + z^2 4x + 2y + 3 = 0$ are
 - (a) (2, -1, 0) and $\sqrt{2}$
 - (b) (2, -1, 0) and 2
 - (c) (2, -1, 0) and 3
 - (d) (-2, 1, 0) and 3
 - (e) (-4, 2, 0) and 3
 - (f) Not enough information or none of the above
- 2. Which of the following is an equation for the straight line through the points (0,1,3) and (4,3,5).
 - (a) $\mathbf{r}(t) = <0, 1, 3 > +t < 4, 3, 5 >$
 - (b) $\mathbf{r}(t) = <0, 1, 3 > -t < 4, 3, 5 >$
 - (c) $\mathbf{r}(t) = <4, 3, 5>+t<8, 4, 4>$
 - (d) $\mathbf{r}(t) = t < 4, 2, 2 >$
 - (e) Not enough information or none of the above
- 3. The length of the curve $\mathbf{r}(t) = \langle 10\sqrt{2}t, e^{10t}, e^{-10t} \rangle$ on the interval $0 \le t \le 1$ is given by
 - (a) $e^5 e^{-5}$
 - (b) $e^{20} + e^{-20}$
 - (c) $e^{10} + e^{-10}$
 - (d) $e^{10} e^{-10}$
 - (e) Not enough information or none of the above
- 4. Let $\mathbf{v} = 3\mathbf{i} + 2\mathbf{k}$ and $\mathbf{w} = 5\mathbf{i} \mathbf{j}$. The vector projection of \mathbf{w} onto \mathbf{v} is
 - (a) $\frac{10}{13} < 3, 2, 0 >$
 - (b) $\frac{15}{13} < 3, 0, 2 >$
 - (c) $\frac{10}{13}$ < 5, -1, 0 >
 - (d) $\frac{10}{\sqrt{13}}$ < 3, 2, 0 >
 - (e) Not enough information or none of the above
- 5. The angle between the vectors $\mathbf{a} = <1, 1, 0>$ and $\mathbf{b} = <0, 2, -2>$ is
 - (a) $\pi/3$
 - (b) $\pi/6$
 - (c) $\pi/4$
 - (d) $\pi/2$
 - (e) Not enough information or none of the above

- 1. True/False. Must CIRCLE the correct answer to receive credit.
 - (a) The magnitude of the cross product of a magnitude 4 vector and a magnitude 7 vector is always 28.
 - true
 - false
 - (b) The line $\mathbf{r}(t) = <3, -1, 4>+t<6, -2, 6>$ passes through the origin.
 - true
 - false
 - (c) If \mathbf{a} , \mathbf{b} , and \mathbf{c} are vectors in \mathbb{R}^3 , and $\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \cdot \mathbf{c}$, then \mathbf{b} and \mathbf{c} differ by a vector that is parallel to \mathbf{a} .
 - true
 - false
 - (d) Suppose a particle moves on a sphere centered at the origin in \mathbb{R}^3 . That means that if $\mathbf{r}(\mathbf{t})$ is the vector function that describes the particle's trajectory, the $|\mathbf{r}(\mathbf{t})|$ is constant. Then the particle's velocity must be parallel to its position vector at all times.
 - true
 - false
- 1. (24 points) A hot air balloon is flying at a constant altitude of 500 meters above the ground, and at a constant speed of 5 meters per second. Someone drops a rock from the balloon. Ignoring friction, and using g = 10 (meters/second²), find the velocity and speed at which the rock hits the ground. (Model the situation by using an xy-coordinate system in which the x axis represents the ground, the balloon's location is y = 500 and its movement is in the positive x direction).

| 2. | (25 points) All following questions refer to a particle whose trajectory in time is given by $\mathbf{r}(t) = <3\cos t, 2\sin t, \sqrt{5}\sin t>$, $0 \le t \le 2\pi$. The unit of length is meters and the unit of time is seconds. |
|----|--|
| | (a) Find the speed at $t = \pi$. |
| | |
| | (b) Find the unit tangent vector at $t = \pi$. |
| | (c) What is the angle between the acceleration and velocity vectors at all times? |
| | |