

Zeros of a Polynomial – Sections 2.3-2.5

Algebraically solve the following equations:

1. $x^3 - 7x^2 + 11x = 0$
2. $2x^3 + 3x^2 - 89x + 120 = 0$
3. $x^3 - 3x^2 - x + 3 = 0$

Zeros and Multiplicities – Section 2.3

Algebraically find all the zeros and their multiplicities for the following functions:

4. $f(x) = 2x^3 - 3x^2 - 12x + 20$
5. $f(x) = x^3 - 3x + 2$
6. $f(x) = 3x^3 + 22x^2 + 15x - 100$

End Behavior of Polynomials – Section 2.3

Use the leading coefficient test to determine the end behavior of the following polynomial functions:

7. $f(x) = -2x^3 + x - 2$
8. $f(x) = -x^{10} - 3x^9 + x^2$
9. $f(x) = 2x^3 + x - 2$

Long or Synthetic Division – Section 2.4

Divide the following using long or synthetic division:

10. $\frac{2x^4 - 6x^2 + 1}{x + 1}$
11. $\frac{4x^2 - 8x + 1}{2x - 1}$
12. $\frac{2x^3 - 7x^2 + 2x + 3}{x - 3}$

Vertical Asymptotes – Section 2.6

Find the equation of the vertical asymptotes (if any) of the following functions:

13. $f(x) = \frac{3x + 2}{x^2 - 1}$
14. $f(x) = \frac{x + 4}{3x + 1}$
15. $f(x) = \frac{x + 2}{x^2 - 4}$

Applications of Rational Functions – Section 2.6

16. The following rational function in hundreds models the population of a certain species of animal, where t is measured in days. What number does the population approach in the long run?

$$p(t) = \frac{10t^3 + 2}{2t^3 + 1}$$

17. The average cost of producing a popular board game is given by the function:

$\bar{C}(x) = \frac{1500 + 15x}{x}$, $x \geq 0$, when x is the number of the board game sold, identify the horizontal asymptote of the function and explain its meaning in this context.

18. The function $N(t) = \frac{0.8t + 100}{5t + 4}$, $t \geq 15$, gives the body concentration $N(t)$, in parts per million of a certain dosage of medication after time t , in hours. Find the horizontal asymptote of the graph and explain the meaning in the context of the problem.

Rewrite in the equivalent logarithmic form – Section 3.1

19. $a^{x+1} = 65$

20. $e^{3x} = 5$

Rewrite in the equivalent exponential form – Section 3.2

21. $\log_6(4x) = 10$

22. $\ln(B) = A$

Compound interest – Section 3.4

23. Find the accumulated value of an investment of \$21,000 at an interest rate of 5.6% for 7 years:

a) compounded monthly

b) compounded continuously

24. a) What initial investment at 3.75% interest compounded continuously for 10 years will accumulate to \$20,000? Round your answer to the nearest cent.

b) What initial investment at 4.25% interest compounded monthly for seven years will accumulate to \$20,000? Round your answer to the nearest cent.

Properties of Logarithms – Section 3.3

Use properties of logarithms to write as a sum or difference logarithms with no exponents.

25. $\log\left(\frac{x^5 y^7}{z^3}\right)$

26. $\ln\left((x-1)^{\frac{3}{2}} \sqrt{\frac{(y+3)^4}{z^8}}\right)$

Use properties of logarithms to express the following as a single logarithms

27. a) $2\ln(x) - 5\ln(y) + 9\ln(w)$

b) $\frac{3}{2}\ln(x+3) - \ln(x) - \frac{1}{2}\ln(x+3)$

28. a) $3\log(A) - 4\log(B) + 5\log(C) - 6\log(D)$

b) $\log(8) + \log(x^2 - 1) - \log(x) - \log(x+1)$

Exponential Equations – Section 3.4

Solve the following for x

29. a) $2^{2x+17} = 8$

b) $10e^{3x-7} = 5$

30. a) $e^{2x} + 2e^x - 35 = 0$

b) $(7)^{2x} + 2(7)^x - 15 = 0$

c) $2e^{2x} + 3e^x - 20 = 0$

Domain of Logarithms function – Section 3.2

Find the domain of the following function;

31. a) $f(x) = \ln(6 - 2x)$

b) $f(x) = \log(4x + 16)$

Logarithms Equations – Section 3.4

32. a) Find the x -intercept of the following function $f(x) = 4 - 2\log_3(2x - 10)$

b) Find the y -intercept of the function $f(x) = \ln(2x + 3)$

33. Solve the following for x :

a) $\log_6(x) - \log_6(x - 5) = 2$

b) $\ln(x) + \ln(2x + 1) = 0$

More with polynomials and zeros – Section 2.5

34. Identify the zeros and the multiplicities of each zero for $f(x) = -2x^4(x + 3)^2(x - 7)^8$.

35. Construct a degree 4 polynomial with real coefficients with zeros at $3i$ (multiplicity 1), -4 (multiplicity 2) and with leading coefficient of 1.

36. Construct a degree 3 polynomial with real coefficients, with zeros at $2 + 3i$ (multiplicity 1), 5 (multiplicity 1), and with leading coefficient of 1.

37. Find all possible rational zeros from the conclusion of the Rational Root Theorem for the polynomial $f(x) = 2x^4 - x^3 + 2x + 21$

More with rational functions – Section 2.6

38. Construct a rational function with the following characteristics:

i. x -intercepts at $(2,0)$ and $(7,0)$

ii. vertical asymptotes at $x = 4$ and $x = -5$

iii. horizontal asymptote at $y = 9$

Answers

1. $0, \frac{7}{2} \pm \frac{1}{2}\sqrt{5}$ 2. $5, -8, \frac{3}{2}$ 3. $1, -1, 3$

4. zero at $\frac{-5}{2}$ mult. 1 and zero at 2 mult. 2

5. zero at -2 with mult. 1 and zero at 1 with mult. 2

6. zeros at -4 , $\frac{5}{3}$, -5 with mult. of 1 for each.

7. rises left, falls right

8. falls left, falls right

9. falls left, rises right

10. Q: $2x^3 - 2x^2 - 4x + 4$ R: -3 11. Q: $2x - 3$ R: -2

12. Q: $2x^2 - x - 1$ R: 0

13. $x = \pm 1$ 14. $x = -\frac{1}{3}$ 15. $x = 2$

16. 5 hundred

17. 15 is the H.A., the average cost when producing a great number of games is \$15.

18. 0.16 ppm is the concentration after a long time.

19. $\log_a(65) = x + 1$

20. $\ln(5) = 3x$

21. $4x = 6^{10}$

22. $B = e^4$

23. a) \$31,050.37

b) \$31,078.69

24. a) \$13,745.79

b) \$14,861.26

25. $5\log(x) + 7\log(y) - 3\log(z)$

26. $\frac{3}{2}\ln(x-1) + 2\ln(y+3) - 4\ln(z)$

27. a) $\ln\left(\frac{x^2w^9}{y^5}\right)$

b) $\ln\left(\frac{x+3}{x}\right)$

28. a) $\log\left(\frac{A^3C^5}{B^4D^6}\right)$

b) $\log\left(\frac{8x-8}{x}\right)$

29. a) -7

b) $\frac{7 + \ln(1/2)}{3} = \frac{7 - \ln(2)}{3} \approx 2.102$

30. a) $\ln 5 \approx 1.609$

b) $\frac{\ln(3)}{\ln(7)} = \log_7(3) \approx 0.56458$

c) $\ln\left(\frac{5}{2}\right) \approx 0.916$

31. a) $(-\infty, 3)$

b) $(-4, \infty)$

32. a) $(\frac{19}{2}, 0)$

b) $(0, \ln 3)$

33. a) $\frac{36}{7}$

b) $\frac{1}{2}$

34. 0, multiplicity 4; -3 , multiplicity 2; 7, multiplicity 8

35. $p(x) = (x^2 + 9)(x + 4)^2$

36. $p(x) = (x - 5)(x^2 - 4x + 13)$

37. $\left\{ \pm 1, \pm \frac{1}{2}, \pm 3, \pm \frac{3}{2}, \pm 7, \pm \frac{7}{2}, \pm 21, \pm \frac{21}{2} \right\}$

38. $r(x) = \frac{9(x-2)(x-7)}{(x-4)(x+5)}$