Name $\qquad$ Recitation Day \& Time $\qquad$

The graph below shows a rate of change function $r$ and an interval from $a$ to $x$. The dots on the $x$ axis indicate the endpoints of intervals that have width $\Delta x$, starting from $a$. Also shown is an approximating constant rate 'step' function created from $r, a$, and $\Delta x$. BEFORE YO BEGIN:
CHANGE THE GRAPH LABEL IN THE ILLUSTRATION FROM $f$ to $r_{f}$.


1. Write expressions for the values described, in terms of $a, x, \Delta x$, and the function $r_{f}$. Do not use any other functions in your answers except $r_{f}$. (You may use $\sum$ with an index like $j$, the floor function, etc.)

Write an expression for the value of....
a) the accumulation due to the first interval, approximated by using the constant rate shown $\qquad$ .
b) $x$ at the left side of the third interval $\qquad$ .
c) the constant rate shown that approximates $r_{f}$ in the second interval $\qquad$ .
d) Draw an arrow on the graph pointing to where you would look to find the value of your answer to part c).
e) What is the total accumulation from the first 80 completed intervals, approximated by using the constant rates shown?
f) How many completed $\Delta x$ intervals are there between $a$ and $x=42.8$ ? $\qquad$ .
g) What is the approximating constant rate in the current interval?

Write your answer without using the word 'left.' .
2. Suppose $x=0.19$ is within the second interval. Still only using $a, x, \Delta x$, and the function $r$, complete the following.
a) Represent the value of $\operatorname{left}(0.19)$ $\qquad$ .
b) Write an expression for the number of completed intervals between $a$ and $x=0.19$, and report the value.

