APM 570 Differential Equations II SS 2021

Horst R. Thieme hthieme@asu.edu

9:00-10:15 am T Th Zoom (presumably) LINE # 12580

This is a basic course on partial differential equations and one of the six core courses of the Ph.D. program in Applied Mathematics.

Topics include

- Method of characteristics, first order quasilinear equations, wave equation, vibrating string.
- Elements of abstract and concrete Fourier series, weak solutions to the vibrating spring equation.
- Heat equation for bounded one-dimensional space, series solutions, maximum principle for arbitrary space dimensions, Green's function.
- Laplace equation on rectangles and disks, maximum principle.
- Applications of Gauß' theorem and Green's formulas to obtain qualitative information on solutions.
- Heat equation on the whole space.

Prerequisites: advanced calculus (like MAT 371), familiarity with partial derivatives, basic knowledge of ordinary differential equations.

Complete notes will be posted on Canvas after each lecture.

Optional background reading:

R. Guenther, J. Lee, Partial Differential Equations of Math. Physics and Integral Eqns. Chap. 1, Sec. 2-1, 2-2, 2-6, 3-1 to 3-5, 4-1 to 4-5, 5-1 to 5-5, 8-1 to 8-4, 9-1 to 9-3, 10-5.

Fritz John, Partial Differential Equations. Fourth edition, Sections 1.1-1.6, 2.3, 2.4, 4.1-4.3.

Course requirements: weekly homework, midterm exam (take home and open notes), and a final exam (take home and open notes).